

# Document indexing, similarities and retrieval in large scale text collections

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# Course objectives

- Introduce the main concepts, models and algorithms for computing indexing text documents and computing similarities in large scale text collections
- We will focus on:
  - Document indexing and representations in large scale collections
  - Standard models for Information Retrieval (IR)
  - PageRank (computing the importance of a page on the Web)
  - Learning to rank models

# Application domains

- Information retrieval
  - Query indexing module
  - Documents indexing module
  - Module to match queries and documents
- Classification
  - Binary, multi-class; mono-/multi-label
  - Flat vs hierarchical
- Clustering
  - Hard vs soft clustering
  - Flat vs hierarchical

# Part 1: Indexing, similarities, information retrieval

## Content

- 1 Indexing
- 2 Standard IR models
- 3 Evaluation

# Indexing steps

## 1 Segmentation

- Segment a text into words:

*the importance of retrieving the good information*  
*the, importance, of, retrieving, the, good, information*

7 words but only 6 word types; depending on languages, may require a dictionary

## 2 Stop-word removal (stop-word list)

## 3 Normalization

- Upper/lower-case, inflected forms, lexical families
- Lemmatization, stemming

→ Bag-of-words: *importance, retriev, inform*

# Vector space representation

- The set of all word types constitute the vocabulary of a collection. Let  $M$  be the size of the vocabulary and  $N$  be the number of documents in the collection  $\rightarrow M$ -dimensional vector space (each axis corresponds to a word type)
- Each document is represented by a vector the coordinates of which correspond to:
  - Presence/absence or number of occurrences of the word type in the doc:  $w_i^d = \text{tf}_i^d$
  - Normalized number of occurrences:  $w_i^d = \frac{\text{tf}_i^d}{\sum_{i=1}^M \text{tf}_i^d}$
  - $tf*idf$ :  

$$w_i^d = \frac{\text{tf}_i^d}{\sum_{i=1}^M \text{tf}_i^d} \underbrace{\log \frac{N}{\text{df}_i}}_{idf_i}$$

where  $\text{df}_i$  is the number of docs in which word (type)  $i$  occurs

# A sparse representation

Most of the words (terms) only occur in few documents and most coordinates of each document are null; storage space is thus saved by considering only words present in documents → **sparse representation**

## Example

$$\text{document } d \left\{ \begin{array}{ll} \text{int } l & \text{(doc length)} \\ \text{ArrWords int}[l] & \text{(sorted word indices)} \\ \text{ArrWeights float}[l] & \text{(word weights)} \\ \dots & \end{array} \right.$$

How to compute a dot product between documents?

# Dot product with sparse representations



# Inverted file

It is possible, with sparse representations, to speed up the comparison between docs by relying on an *inverted file* that provides, for each term, the list of documents they appear in:

$$\text{word } i \left\{ \begin{array}{ll} \text{int } l & \text{(number of docs)} \\ \text{ArrDocs int}[l] & \text{(sorted doc indices)} \\ \dots & \end{array} \right.$$

**Remark** Advantageous with measures (distances, similarities) that do not rely on words not present in docs; dot/scalar product?, cosine?, Euclidean distance?

# Building an inverted file

With a static collection, 3 main steps:

- 1 Extraction of id pairs (*term*, *doc*) (complete pass over the collection)
- 2 Sorting acc. to term id, then doc id
- 3 Grouping pairs corresponding to same term

Easy to implement when everything fits into memory

How to proceed with large collections?

# Insufficient memory

Intermediate "inverted files" are temporarily stored on disk. As before, 3 main steps:

- 1 Extraction of id pairs (*term*, *doc*) (previous algo.) and writing on file *F*
- 2 Reading file *F* by blocks that can fit into memory; inversion of each block (previous algo.) and writing in a series of files
- 3 Merging all local files to create global inverted file

→ *Blocked sort-based indexing* (BSBI) algorithm

# BSBI (1)

- ❶  $n \leftarrow 0$
- ❷ while (some docs have not been processed)
- ❸ do
- ❹  $n \leftarrow n + 1$
- ❺  $\text{block} \leftarrow \text{ParseBlock}()$
- ❻  $\text{BSBI-Invert}(\text{block})$
- ❼  $\text{WriteBlockToDisk}(\text{block}, f_n)$
- ❽  $\text{MergeBlocks}(f_1, \dots, f_n; f_{\text{merged}})$

## BSBI (2)

The inversion (in BSBI) consists in sorting pairs on two different keys (term and doc ids). Complexity in  $O(T \log T)$  where  $T$  represents the number of (term,doc) pairs

### Example

$t_1 = \text{"brutus"} , t_2 = \text{"caesar"} , t_3 = \text{"julius"} , t_4 = \text{"kill"} , t_5 = \text{"noble"}$

$t_1 : d_1$	$t_2 : d_4$	$t_2 : d_1$
$t_3 : d_{10}$	$t_1 : d_3$	$t_4 : d_8$
$t_5 : d_5$	$t_2 : d_2$	$t_1 : d_7$

## Standard IR models

# The different standard models

- Boolean model
- Vector-space model
- Prob. models

# Boolean model (1)

Simple model based on set theory and Boole algebra, characterized by:

- Binary weights (presence/absence)
- Queries as boolean expressions
- Binary relevance
- System relevance: satisfaction of the boolean query



## Boolean model (2)

### Example

$q = \text{programming} \wedge \text{language} \wedge (\text{C} \vee \text{java})$

$(q = [\text{prog.} \wedge \text{lang.} \wedge \text{C}] \vee [\text{prog.} \wedge \text{lang.} \wedge \text{java}])$

	programming	language	C	java	...
$d_1$	3 (1)	2 (1)	4 (1)	0 (0)	...
$d_2$	5 (1)	1 (1)	0 (0)	0 (0)	...
$d_0$	0 (0)	0 (0)	0 (0)	3 (1)	...

### Relevance score

$RSV(d, q) = 1$  iff  $\exists q_{cc} \in q_{dnf}$  s.t. all terms in  $q_{cc}$  are in  $d$ ; 0 otherwise

## Boolean model (3)

### Algorithmic considerations

Sparse term-document matrix: inverted file to select all document in conjonctive blocks (can be processed in parallel) - intersection of document lists

	$d_1$	$d_2$	$d_3$	$\dots$
programming	1	1	0	$\dots$
langage	1	1	0	$\dots$
C	1	0	0	$\dots$
$\dots$	$\dots$	$\dots$	$\dots$	

## Boolean model (4)

### Advantages and disadvantages

- + Easy to implement (at the basis of all models with a union operator)
- Binary relevance not adapted to topical overlaps
- From an information need to a boolean query

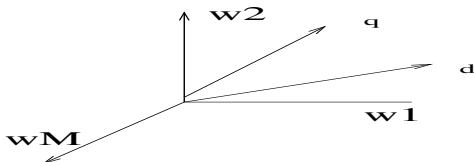
**Remark** At the basis of many commercial systems

## Vector space model (1)

Corrects two drawbacks of the boolean model: binary weights and relevance

It is characterized by:

- Positive weights for each term (in docs and queries)
- A representation of documents and queries as vectors (see before on bag-of-words)



## Vector space model (2)

Docs and queries are vectors in an  $M$ -dimensional space the axes of which corresponds to word types

**Similarity** Cosine between two vectors

$$RSV(d_j, q) = \frac{\sum_i w_i^d w_i^q}{\sqrt{\sum_i (w_i^d)^2} \sqrt{\sum_i (w_i^q)^2}}$$

**Property** The cosine is maximal when the document and the query contain the same words, in the same proportion! It is minimal when they have no term in common (similarity score)

## Vector space model (3)

### Advantages and disadvantages

- + Total order (on the document set): distinction between documents that completely or partially answer the information need
- Framework relatively simple; not amenable to different extensions

*Complexity* Similar to the boolean model (dot product only computed on documents that contain at least one query term)

# Probabilistic models

- *Binary Independence Model* and BM25 (S. Robertson & K. Sparck Jones)
- *Inference Network Model* (Inquery) - *Belief Network Model* (Turtle & Croft)
- *(Statistical) Language Models*
  - *Query likelihood* (Ponte & Croft)
  - *Probabilistic distance retrieval model* (Zhai & Lafferty)
- *Divergence from Randomness* (Amati & Van Rijsbergen) - *Information-based models* (Clinchant & Gaussier)

# Generalities

Boolean model → binary relevance

Vector space model → similarity score

Probabilistic model → probability of relevance

Two points of view: document generation (probability that the document is relevant to the query - BIR, BM25), query generation (probability that the document "generated" the query - LM)



# Introduction to language models: two die

Let  $D_1$  and  $D_2$  two (standard) die such that, for small  $\epsilon$ :

For  $D_1$ ,  $P(1) = P(3) = P(5) = \frac{1}{3} - \epsilon$ ,  $P(2) = P(4) = P(6) = \epsilon$

For  $D_2$ ,  $P(1) = P(3) = P(5) = \epsilon$ ;  $P(2) = P(4) = P(6) = \frac{1}{3} - \epsilon$

Imagine you observe the sequence  $Q = (1, 3, 3, 2)$ . Which dice most likely produced this sequence?

Answer

$$P(Q|D_1) = (\frac{1}{3} - \epsilon)^3 \epsilon; P(Q|D_2) = (\frac{1}{3} - \epsilon) \epsilon^3$$

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## Language model - QL (1)

Documents are die; a query is a sequence → What is the probability that a document (dice) generated the query (sequence)?

$$RSV(q, d) = P(q|d) = P(q_1 \dots q_l | d) = \prod_{j=1}^l P(q_j | d) = \prod_i P(i|d)^{occ(i;q)}$$

where  $occ_i^q$  denotes number of occurrences of word  $i$  in  $q$

How to estimate the quantities  $P(i|d)$ ?

Maximum Likelihood principle  $\Rightarrow p(i|d) = \frac{occ(i;d)}{\sum_i occ(i;d)}$

Problem with query words not present in docs

## Language model - QL (2)

### Solution: smoothing

One takes into account the collection model:

$$p(w|d) = (1 - \alpha_d) \frac{\text{occ}(i;d)}{\sum_i \text{occ}(i;d)} + \alpha_d \frac{\text{occ}(i;\mathcal{C})}{\sum_i \text{occ}(i;\mathcal{C})}$$

Example with Jelinek-Mercer smoothing:  $\alpha_d = \lambda$

- $\mathcal{D}$ : development set (collection, some queries and associated relevance judgements)
- $\lambda = 0$ :
- Repeat till  $\lambda = 1$ 
  - IR on  $\mathcal{D}$  and evaluation (store evaluation score and associated  $\lambda$ )
  - $\lambda \leftarrow \lambda + \epsilon$
- Select best  $\lambda$

## Language model - QL (3)

### Advantages and disadvantages

- + Theoretical framework: simple, well-founded, easy to implement and leading to very good results
- + Easy to extend to other settings as cross-language IR
- Training data to estimate smoothing parameters
- Conceptual deficiency for (pseudo-)relevance feedback

Complexity similar to vector space model

## Evaluation of IR systems

# Relevance judgements

- Binary judgements: the doc is relevant (1) or not relevant (0) to the query
- Multi-valued judgements:  
*Perfect > Excellent > Good > Correct > Bad*
- Preference pairs: doc  $d_A$  more relevant than doc  $d_B$  to the query

Several (large) collections with many ( $> 30$ ) queries and associated (binary) relevance judgements: TREC collections ([trec.nist.gov](http://trec.nist.gov)), CLEF ([www.clef-campaign.org](http://www.clef-campaign.org)), FIRE ([fire.irsil.res.in](http://fire.irsil.res.in))

# Common evaluation measures

- MAP (Mean Average Precision)
- MRR (Mean Reciprocal Rank)
  - For a given query  $q$ , let  $r_q$  be the rank of the first relevant document retrieved
  - MRR: mean of  $r_q$  over all queries
- WTA (Winner Takes All)
  - If the first retrieved doc is relevant,  $s_q = 1$ ;  $s_q = 0$  otherwise
  - WTA: mean of  $s_q$  over all queries
- NDCG (Normalized Discounted Cumulative Gain)



# NDCG

- NDCG at position  $k$ :

$$N(k) = \underbrace{Z_k}_{\text{normalization}} \underbrace{\sum_{j=1}^k}_{\text{cumul}} \underbrace{(2^{p(j)} - 1)}_{\text{gain}} / \underbrace{\log_2(j+1)}_{\text{position discount}}$$

- Averaged over all queries

## G : Gain

Relevance	Value (gain)
<i>Perfect (5)</i>	$31 = 2^5 - 1$
<i>Excellent (4)</i>	$15 = 2^4 - 1$
<i>Good (3)</i>	$7 = 2^3 - 1$
<i>Correct (2)</i>	$3 = 2^2 - 1$
<i>Bad (0)</i>	$0 = 2^1 - 1$

# DCG : Discounted CG

Discounting factor:  $\frac{\ln(2)}{\ln(j+1)}$

Doc. (rg)	Rel..	Gain	CG	DCG
1	<i>Perf.</i> (5)	31	31	31
2	<i>Corr.</i> (2)	3	$34 = 31 + 3$	$32,9 = 31 + 3 \times 0,63$
3	<i>Exc.</i> (4)	15	49	40,4
4	<i>Exc.</i> (4)	15	64	46,9
...	...	...	...	...

# Ideal ranking: max DCG

Document (rank)	Relevance	Gain	max DCG
1	<i>Perfect (5)</i>	31	31
3	<i>Excellent (4)</i>	15	40,5
4	<i>Excellent (4)</i>	15	48
...	...	...	...

# Normalized DCG

Doc. (rang)	Rel.	Gain	DCG	max DCG	NDCG
1	<i>Perfect (5)</i>	31	31	31	1
2	<i>Correct (2)</i>	3	32,9	40,5	0,81
3	<i>Excellent (4)</i>	15	40,4	48	0.84
4	<i>Excellent (4)</i>	15	46,9	54,5	0.86
...	...	...	...	...	

## Remarks on evaluation measures

- Measures for a given position (e.g. list of 10 retrieved documents)
- NDCG is more general than MAP (multi-valued relevance vs binary relevance)
- Non continuous (and thus non derivable)